

# Non-linear control model for use in greenhouse climate control systems

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## Electronic supplementary material (ESM)

Appendix A:

The parameters of the derived control law:

$$\begin{aligned}\pi_1 = & S_i U_A^2 T_r \alpha + S_i U_A^2 \alpha e_{e_1} + \beta_T H_{out} \lambda U_A^2 T_r - \beta_T H_{out} \lambda U_A^2 e_{e_1} - \beta_T \lambda U_A^2 T_r H_r - \beta_T \lambda U_A^2 T_r e_{e_2} - \beta_T \lambda U_A^2 H_r e_{e_1} - \\ & - \beta_T \lambda U_A^2 e_{e_1} e_{e_2} - \beta_T C_p \lambda S_i H_r \rho - \beta_T^2 C_p \lambda S_i e_{e_2} \rho + \beta_T^2 C_p \lambda U_A T_r H_r \rho + \beta_T^2 C_p \lambda U_A T_r e_{e_2} \rho + \beta_T^2 C_p \lambda U_A H_r e_{e_1} \rho + \\ & + \beta_T^2 C_p \lambda U_A e_{e_1} e_{e_2} \rho - \beta_T C_p \lambda S_i V_H \rho V_2 + C_p S_i U_A V_T \alpha \rho V_1 + \beta_T C_p H_{out} \lambda U_A V_T \rho V_1 + \beta_T C_p \lambda U_A V_H T_r \rho V_2 - \\ & - \beta_T C_p \lambda U_A V_T H_r \rho V_1 + \beta_T C_p \lambda U_A V_H e_{e_1} \rho V_2 - \beta_T C_p \lambda U_A V_T e_{e_2} \rho V_1\end{aligned}$$

$$\pi_2 = \lambda \left( \beta_T \lambda U_A H_r - \beta_T H_{out} \lambda U_A - S_i U_A \alpha + \beta_T \lambda U_A e_{e_2} - \beta_T C_p S_i \rho + \beta_T C_p U_A T_r \rho + \beta_T C_p U_A e_{e_1} \rho \right)$$

$$\pi_3 = \beta_T U_A \left( U_A T_r + U_A e_{e_1} + \beta_T \lambda H_r + \beta_T \lambda e_{e_2} + \lambda V_H V_2 + C_p V_T \rho V_1 \right)$$

$$\pi_4 = \beta_T \lambda U_A H_r - \beta_T H_{out} \lambda U_A - S_i U_A \alpha + \beta_T \lambda U_A e_{e_2} - \beta_T C_p S_i \rho + \beta_T C_p U_A T_r \rho + \beta_T C_p U_A e_{e_1} \rho$$

where:  $V_1 = G_{ET}(e_{e_1}) + G_{EIT} \times \sum_{t \rightarrow \infty} (e_{e_1})$  and  $V_2 = G_{EH}(e_{e_2}) + G_{EIH} \times \sum_{t \rightarrow \infty} (e_{e_2})$  – the parameters used for the stability of the closed-loop system. The parameters  $G_{ET}$  and  $G_{EIT}$  – the control gains of the temperature error response and the temperature error integral, respectively. As well,  $G_{EH}$  and  $G_{EIH}$  – the control gains of the relative humidity error response and the relative humidity error integral, respectively.

Appendix B:

The system equations can be written as:

$$\dot{x} = F(x, v) + G(x, v)u$$

$$F(x, v) = \begin{bmatrix} -\frac{U_A}{\rho C_p V_T} T_{in} + \frac{1}{\rho C_p V_T} S_i + \frac{U_A}{\rho C_p V_T} T_{out} \\ \alpha S_i \end{bmatrix} \quad G(x, v) = \begin{bmatrix} -\frac{1}{t_v} (T_{in} - T_{out}) & -\frac{\lambda Q_{fog}}{\rho C_p V_T} \\ -\frac{1}{t_v} (H_{in} - H_{out}) & \frac{1}{V_H} \end{bmatrix}$$

$$u = \left[ \frac{V_r \%}{Q_{fog} \%} \right]^T$$

where:  $t_v$  – the inverse of the number of air changes per unit time.

The equivalent control law can be written as:

$$u = G^{-1}(x, v) [-F(x, v) + r]$$

The compensate sliding mode control law ( $r$ ) can be expressed as:

$$r_i = -a_{4i}^{-1} \left( k_i s_i + \varepsilon_i \operatorname{sgn}(s_i) + a_{4i} \hat{D}_{1i} - a_{4i} \dot{x}_{Ti} + a_{5i} e_i \right)$$

where:  $s_i = a_{4i} e_i + a_{4i} \sigma_{0i} + \int_0^t a_{5i} e_i dt$  – the sliding surface;  $i$  – temperature, humidity.

$\hat{D}_{1i}$  can be expressed as:

$$\ddot{\hat{D}}_{1i} = -L_i^{-1} \left( \ddot{\sigma}_{0i} + a_{1i} \sigma_{1i} + a_{2i} \operatorname{sgn}(\sigma_{1i}) + \hat{a}_{3i} \operatorname{sgn}(\sigma_{1i}) \right)$$

$$\sigma_{1i} = \sigma_{0i} + L_i \ddot{\sigma}_{0i}$$

$$\sigma_{0i} = z - e_i$$

$$\dot{z} = r_1 + \hat{D}_{1i} - \dot{x}_{Ti}$$

$$e_i = x_i - \dot{x}_{Ti}$$

$$\ddot{\hat{a}}_3 = \gamma_{0i} |\sigma_{1i}|$$

where:  $x$  and  $x_T$  – the state vector and reference vector, respectively.

The constant parameters can be written as in Table S1.

Table S1. Constant parameters of the integral sliding mode control system

| $i$         | $a_1$ | $a_2$ | $a_4$ | $a_5$ | $k$  | $\varepsilon$ | $L$ | $\gamma_0$ |
|-------------|-------|-------|-------|-------|------|---------------|-----|------------|
| Temperature | 0.02  | 0.03  | 100   | 0.01  | 0.08 | 0.8           | 0.5 | 0.05       |
| Humidity    | 0.01  | 0.01  | 100   | 0.008 | 0.5  | 2             | 1   | 0.02       |